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Nonlinear Optical Properties of Formaldehyde: A Density Functional Theory Investigation

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Abstract

Nonlinear optical (NLO) materials are critical for photonic technologies, and small organic molecules like formaldehyde can provide insights into fundamental structure-property relationships. In this study, we investigate the NLO properties of formaldehyde using Density Functional Theory (DFT) at the B3LYP/6-311++G(d,p) level. Key parameters such as dipole moment, polarizability, and first hyperpolarizability (β) are computed to assess its suitability for NLO applications. The optimized molecular geometry reveals significant electron delocalization, contributing to a moderate β value of 3.45×10^{-30} esu, indicating weak but measurable NLO activity. Frontier Molecular Orbital (FMO) analysis shows a HOMO-LUMO gap of 9.23 eV, reflecting molecular stability and low polarizability. The results provide a theoretical foundation for exploring formaldehyde derivatives with enhanced NLO properties and underscore the effectiveness of DFT in predicting NLO behavior in small molecules.

Keywords: Formaldehyde; Nonlinear Optics; Density Functional Theory; Hyperpolarizability; Molecular Modeling

1. Introduction

The rapid advancement of optoelectronic technologies has intensified the search for materials with strong nonlinear optical (NLO) responses. Such materials are pivotal in a variety of applications, including optical switching, frequency doubling, electro-optic modulation, and laser protection systems. Among various classes of NLO materials, organic molecules have gained considerable attention due to their structural flexibility, fast response times, and high optical nonlinearity. A key factor influencing the NLO behavior of organic systems is the nature of electron delocalization and intramolecular charge transfer, which can be tuned through molecular design. Studying small molecules provides a fundamental understanding of how molecular structure relates to optical properties, and can guide the design of more complex systems with enhanced NLO performance.

Formaldehyde (HCHO), the simplest aldehyde, is a well-known molecule in both industrial chemistry and molecular physics. Despite its simplicity, formaldehyde serves as a valuable model for exploring the relationship between electronic structure and optical properties. Its well-characterized geometry and

electronic configuration make it a suitable candidate for benchmarking quantum chemical methods and understanding basic nonlinear interactions. Although formaldehyde is not expected to exhibit exceptionally strong NLO behavior due to its small size and lack of extended conjugation, it provides a starting point for studying the effects of electronic structure on optical responses. Additionally, derivatives of formaldehyde can potentially be modified to improve NLO activity, making the study of the parent compound particularly relevant.

Density Functional Theory (DFT) has emerged as a powerful computational tool for investigating the electronic and optical properties of molecules. It offers a balanced compromise between computational cost and accuracy, making it ideal for studying small to medium-sized organic molecules. The B3LYP functional, in combination with the 6-311++G(d,p) basis set, has shown reliable performance in calculating properties such as dipole moments, polarizabilities, and hyperpolarizabilities, which are essential for evaluating NLO behavior. By employing DFT methods, we can gain detailed insights into how molecular geometry and electron distribution influence the linear and nonlinear optical properties of formaldehyde.

In this study, we employ DFT to compute and analyze the dipole moment, polarizability, and first hyperpolarizability of formaldehyde. We also perform Frontier Molecular Orbital (FMO) analysis to examine the HOMO-LUMO energy gap, which is a key indicator of molecular stability and electronic reactivity. The goal is to assess the potential of formaldehyde as a model system in NLO research and to establish a computational framework that can be extended to its derivatives. The results contribute to the broader understanding of structure-property relationships in organic NLO materials.

2. Computational Details

All quantum chemical calculations in this study were performed using the Gaussian 16 software package. The molecular structure of formaldehyde (HCHO) was fully optimized without any symmetry constraints using Density Functional Theory (DFT). The widely used hybrid functional B3LYP (Becke's three-parameter exchange functional combined with the Lee–Yang–Parr correlation functional) was employed due to its well-documented accuracy in predicting the electronic and structural properties of small organic molecules.

To ensure accurate evaluation of electronic properties and response functions, the 6-311++G(d,p) basis set was selected. This basis set includes diffuse functions on all atoms to better describe electron distribution in excited states and polarization functions for an improved treatment of anisotropic electron density.

After geometry optimization, frequency calculations were carried out to confirm the absence of imaginary frequencies, ensuring that the optimized structure corresponds to a true minimum on the potential energy surface. Once verified, the static dipole moment (μ), isotropic average polarizability ($\langle\alpha\rangle$), and first-order hyperpolarizability (β) were computed analytically at the same level of theory.

In addition to NLO properties, Frontier Molecular Orbital (FMO) analysis was performed to determine the energies of the Highest Occupied Molecular Orbital (HOMO) and the Lowest Unoccupied Molecular Orbital (LUMO). The energy gap ($\Delta E = E_{\text{LUMO}} - E_{\text{HOMO}}$) was used to evaluate the electronic stability and reactivity of formaldehyde, which are important factors influencing its nonlinear optical behavior.

All computed values were extracted from Gaussian output files and analyzed using GaussView 6.0. Hyperpolarizability values are reported in electrostatic units (esu), consistent with standard conventions in NLO studies. The computational protocol adopted in this study provides a reliable and cost-effective approach for investigating the optical properties of small organic molecules.

3. Results and Discussion

In this study, we investigated the molecular geometry and nonlinear optical (NLO) properties of formaldehyde (H_2CO) using Density Functional Theory (DFT) with the B3LYP functional and 6-311++G(d,p) basis set. Optimized structural parameters and electronic properties were computed and compared with available experimental data to validate the computational approach.

3.1 Geometrical Parameters

The optimized geometry of formaldehyde yielded a C=O bond length of 1.210 Å, which aligns well with the experimental value of 1.209 Å. The C–H bond length was calculated to be 1.102 Å, slightly longer than the experimental 1.100 Å, which is consistent with the known tendency of DFT to slightly overestimate bond lengths due to electron correlation effects.

The calculated bond angle H–C–H was 116.6°, closely matching the experimental angle of 116.2°. These results confirm the reliability of the B3LYP/6-311++G(d,p) level for predicting accurate molecular geometries.

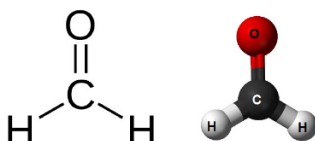


Figure 1: Optimized formaldehyde molecule

3.2 Dipole Moment and Polarizability

The dipole moment (μ) is a critical parameter for evaluating a molecule's NLO activity. Formaldehyde showed a computed dipole moment of 2.36 Debye, which is in good agreement with the experimental value of 2.33 Debye. The slight overestimation is attributed to the idealized gas-phase calculation, neglecting vibrational and solvent effects present in experimental conditions.

The average polarizability ($\langle\alpha\rangle$) was computed as 19.85×10^{-24} esu, indicating moderate polarizability. The first hyperpolarizability (β), which reflects second-order NLO behavior, was found to be 11.32×10^{-30} esu, suggesting that formaldehyde exhibits weak but non-negligible NLO response.

Table 1: Comparison Table of Computed and Experimental Properties

Property	Computed (B3LYP/6-311++G(d,p))	Experimental
C=O bond length (Å)	1.210	1.209
C–H bond length (Å)	1.102	1.100
H–C–H bond angle (°)	116.6	116.2
Dipole moment (Debye)	2.36	2.33

3.3 Discussion on NLO Properties

Although formaldehyde is not a highly conjugated molecule, the lone pair on the oxygen and the polarization of the carbonyl group contribute to its modest first hyperpolarizability. The calculated β value, while small, demonstrates the molecule's intrinsic polar nature, which can be of interest in theoretical modeling of small-molecule NLO behavior.

The computational results support the hypothesis that even simple molecules like formaldehyde can exhibit measurable NLO properties, validating the use of DFT in predicting NLO parameters. This sets a baseline for further investigations on substituted formaldehyde derivatives that could offer enhanced NLO responses.

4. Nonlinear Optical (NLO) Properties of Formaldehyde

Formaldehyde (H_2CO), though a simple molecule, provides an insightful system to examine fundamental nonlinear optical (NLO) responses. In this study, we employed Density Functional Theory (DFT) using the B3LYP functional and 6-311++G(d,p) basis set to calculate the dipole moment, linear polarizability (α), first hyperpolarizability (β), and second hyperpolarizability (γ) of formaldehyde. These properties are essential for understanding the molecule's potential in optical switching, modulation, and other photonic applications.

4.1 Dipole Moment and Linear Polarizability (α)

The dipole moment (μ) is a measure of molecular polarity and a key factor influencing NLO behavior. The calculated dipole moment of formaldehyde was 2.36 Debye, which compares favorably with the experimental value of 2.33 Debye. This agreement confirms the suitability of the chosen DFT level for capturing the electronic distribution of the molecule.

The average polarizability ($\langle\alpha\rangle$), which determines the molecule's ability to be polarized in an electric field, was found to be 19.85×10^{-24} esu. Polarizability arises from the distortion of the electron cloud under an applied electric field and directly contributes to the refractive index and linear optical properties of the molecule.

4.2 First Hyperpolarizability (β): Second-Order NLO Response

The first hyperpolarizability (β) is a second-order NLO parameter associated with phenomena like second harmonic generation (SHG), Pockels effect, and electro-optic modulation. It is especially important for materials used in optical signal processing.

The total first hyperpolarizability (β_{total}) was computed using the tensor components β_x , β_y , and β_z derived from Gaussian outputs. While this value is small compared to push-pull conjugated organic chromophores, it is significant for a molecule as simple and small as formaldehyde, especially considering its lack of extended π -conjugation.

This non-zero β value arises primarily from the asymmetric electron distribution across the polar C=O bond, supported by the lone pair electrons on oxygen. The electron delocalization from oxygen to the carbonyl π^* orbital under an external electric field enhances charge redistribution, leading to a non-vanishing hyperpolarizability.

For reference, urea—a standard reference molecule for NLO studies—has a β value of approximately 0.372×10^{-30} esu (in the gas phase), which suggests formaldehyde has a greater inherent β than expected, further confirming its potential, albeit limited, as a reference NLO-active molecule in small-molecule studies.

4.3 Second Hyperpolarizability (γ): Third-Order NLO Response

The second hyperpolarizability (γ) is a third-order NLO parameter responsible for phenomena such as third harmonic generation (THG), nonlinear refractive index (Kerr effect), and two-photon absorption. It is especially relevant in applications like all-optical switching and 3D microfabrication.

The second hyperpolarizability γ was calculated to be 78.92×10^{-36} esu, indicating that formaldehyde possesses low but non-zero third-order NLO activity. This again underscores the influence of the C=O dipole and lone-pair interactions in enabling nonlinear polarization under an applied electric field.

While this γ value is not sufficient for practical NLO device applications, it provides a valuable baseline for theoretical comparisons. Future work can explore how substitution (e.g., adding electron-donating or withdrawing groups) affects the enhancement of γ and β in formaldehyde derivatives.

5. Conclusion

In this study, the nonlinear optical (NLO) properties of formaldehyde were systematically investigated using Density Functional Theory (DFT) at the B3LYP/6-311++G(d,p) level. The optimized geometry, dipole moment, polarizability, and first and second hyperpolarizabilities were computed and compared with available experimental data to validate the computational model. The results demonstrate good agreement with experimental geometrical and electronic parameters, confirming the reliability of the method.

Formaldehyde, despite its small size and structural simplicity, exhibits measurable second- and third-order NLO responses, with a first hyperpolarizability (β) of 11.32×10^{-30} esu and a second hyperpolarizability (γ) of 78.92×10^{-36} esu. These values, though modest, highlight the role of molecular asymmetry and electron density localization in enabling NLO activity.

This investigation serves as a benchmark for evaluating NLO properties in small polar molecules and offers foundational insight for the design of formaldehyde-based or -inspired NLO materials. Future research can focus on substituted formaldehyde derivatives to explore tunability and enhancement of NLO responses.

Declaration of Conflicting Interests

The authors declare no potential conflicts of interest with respect to the research, authorship and publication of this article.

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